Quantum-chemical study of molecular structure and relative stability of *trans* and *cis* isomers of model anilide derivatives

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Abstract: Derivatives of anilide were studied systematically by the density functional theory (DFT) using the B3LYP hybrid functional and the 6-311+G(3df,2p) basis set. Characteristic frequencies of N—H and C=O stretching modes for *cis* and *trans* conformers distinguishing were compared with available experimental and theoretical data. Effect of substitution in *ortho* position and acidic residue group is discussed with respect to the bond length changes in the aromatic ring and aromaticity indexes. Energy differences between *cis* and *trans* conformations allow estimating the effect of intramolecular hydrogen bonds stabilizing the studied conformations. The *trans* conformation of parent formanilide is stabilized *via* the $C_{\text{(aromatic)}}\text{—H}\cdots\text{O}=\text{C}$ interaction with the energy of around $4\text{ kJ}\cdot\text{mol}^{-1}$. The selected anilide series represent model compounds for drug design.

Keywords: HOMED parameters, acetanilide, aromaticity, steric effect, hydrogen bonding

Introduction

One of the most important linkages in nature is the peptide bond (amide bond) binding amino acids in the formation of proteins. In recent years, formanilide has been the subject of many studies because it is the simplest aromatic molecule including a peptide bond —NH—CO— in its structure. Secondary amides like formanilide are great theoretical models for studying conformational isomerism of the mentioned peptide group (Marochkin and Dorofeeva, 2012). Pure *cis* and *trans* isomers of secondary amides (o-methylformanilide) have been isolated by Siddal et al. for the first time (Siddal et al., 1968). Also, *ab initio* quantum mechanical calculations were used to study the relative stability of the two conformers of selected anilide derivatives by Ilieva (Ilieva et al., 1999).

Various anilide derivatives are successfully used in pharmacy, including the most popular paracetamol and lidocaine pills. By modification of the molecule through substitution, its properties can be modified to fit specific needs. Substitution can invoke significant changes in the molecular structure and various pharmacokinetic and pharmacodynamic parameters including hydrophobicity, acidity, solubility, reactivity and stability. In this task, quantitative description of the effect of various substitutions is crucial. In case of formanilide or acetanilide, the characteristic coplanar structure of the aromatic ring and the amidic bond exhibit *cis* or *trans* geometry. Planarity of this system depends mainly on the substituents in *ortho*-positions of the aromatic

ring. Moreover, also *cis/trans* equilibrium is affected and can also be modified by substituting the acid residue of the amidic bond. Formation of intramolecular hydrogen bonds considerably affects the stability of these isomers as well.

To quantitatively describe the effect of substitution on the aromatic ring, the Hammett equation is usually applied. The Hammett equation (and its extended forms) describes a linear free-energy relationship relating reaction rates and equilibrium constants for many reactions involving benzoic acid derivatives with *meta*- and *para*-substituents (Muller, 2009). Hammett constants can be successfully used for the prediction of equilibrium and rate constants for a variety of reactions (Hansch et al., 1991; Krygowski and Stępień, 2005). Unfortunately, the Hammett equation does not account for steric effects, which are dominant in *ortho* substitution. For this case, a modification of the Hammett constant has been developed by Taft (Taft, 1953).

Aromaticity of the ring as another important parameter can be quantified by the means of geometry changes. Geometry-based new parametrization for the Harmonic Oscillator Model of Aromaticity (HOMA) index was defined more than 30 years ago (Frizzo and Martins, 2012) to determine aromaticity of various types of molecules. π -Electron delocalization in homo- and heteroaromatic systems can be described by this model. The concept of HOMA was taken by Jug and Koester in 1993 to propose reformulated HOMA (rHOMA), which has been applied to various cyclic and acyclic conjugated systems (Jug and Koester, 1990). Discrepancies of the rHOMA

index led Raczyńska et al. to introduce a new Harmonic Oscillator Model of Electron Delocalization (HOMED) index (Raczyńska et al., 2010). Quantum mechanical methods have been used to estimate the bond lengths for the reference molecules as well as for the different π -electron delocalized acyclic and cyclic compounds containing C—C, C—N and C—O bonds including heteroaromatic systems. This method is more advantageous due to the error cancellation during the procedure of the HOMED estimation. In the next modification, normalization constant, α , is calculated using the HOMED theory for systems containing the same number of single and double bonds (even number of bonds). In 2011, the new parametrization for the HOMA index to determine aromaticity of heterocycles was introduced (Frizzo and Martins, 2011) describing HOMA for Heterocycle Electron Delocalization (HOMHED). This theory is based on the experimental data of reference molecules obtained from electron diffraction X-ray measurements.

With respect to the previously published works, the aim of our work was to present energetics of the conformational isomerism of selected model derivatives of anilide using the density functional theory (DFT). Atom numbering and molecular structures of the studied compounds are presented in Fig. 1. In this study, we focused on the substitution in *ortho* position and in acidic residue group to alter the properties of the anilide bond. Based on the normal modes analysis of optimal geometries, the characteristic frequencies distinguishing *cis* and *trans* conformers were determined and compared with available experimental and theoretical data. Finally, the role of intramolecular hydrogen bonds and steric effect of the substituents was analyzed.

Computational details

All calculations were performed using the Gaussian 09 program package (Frisch et al., 2013). Density functional theory (DFT) with the hybrid exchange-correlation B3LYP functional (Becke's three

parameter, Lee-Yang-Parr) (Lee et al., 1988; Becke, 1988) combination were applied. Geometries of studied molecules were optimized in the gas-phase using the 6-311+G(3df,2p) basis set without fixing any internal coordinates. Final structures were confirmed to be real minima by vibrational analysis (no imaginary frequency). Visualization was done using the Molekel program package (Flukiger et al., 2000). Theoretical frequencies of the N—H and C=O stretching modes were obtained by vibrational analysis. Corrected values were calculated by multiplying calculated frequencies by a correction factor of 0.8933. π -Electron delocalization of the studied derivatives of formanilide was determined by HOMED parameters

$$\text{HOMED} = 1 - \frac{1}{n} \alpha_{\text{CC}} \sum \left[(R(\text{CC})_i - R_i)^2 \right] \quad (1)$$

where parameter R_i is the i -th bond length in the studied aromatic ring. In case of an even number of bonds, the normalization constant, α_{CC} , from the HOMED theory reduces to the rHOMA normalization constant, α (Raczyńska et al., 2010). The normalization constant, α , for each type of bond was calculated according to the rHOMA theory from Eq. 2 (Frizzo and Martins, 2012)

$$\alpha = 2 \{ (R_o - R_s)^2 + (R_o - R_d)^2 \}^{-1} \quad (2)$$

where R_o is the reference conjugated bond length in optimized geometry of an ideal aromatic molecule, benzene, R_s is the reference single bond length in ethane and R_d is the reference double bond length in ethene. Values found for the normalization constant, α , for each type of bond were calculated using the values of reference bond lengths ($R_o = 1.391 \text{ \AA}$, $R_s = 1.527 \text{ \AA}$ and $R_d = 1.325 \text{ \AA}$) obtained from the optimized geometry of benzene, ethane and ethene using the same DFT approach as for the studied molecules. HOMED parameters are based on the optimal bond lengths obtained from quantum chemical calculations, while the rHOMA theory employs bond lengths determined by X-ray diffraction.

Fig. 1 Schematic structures, atom numbering and notation of studied *trans* and *cis* isomers.

Results and Discussion

From the structural point of view, formanilide represents a parent molecule (Fig. 1). For the *ortho* substitution, fluorine atom as an electron withdrawing atom is sterically almost identical to hydrogen and thus, intramolecular steric effect is minimized. On the other hand, as the electron donor substituent, methyl group was selected as the smallest candidate with the smallest steric effect. Intramolecular hydrogen bonding was studied by electron withdrawing or electron donor R_3 substitution to modulate the strength of these bonds (Tab. 1). Non-substituted formanilide and acetanilide have co-planar geometry due to extended electron conjugation between the aromatic ring nitrogen lone pair and the C=O group. This conjugation can be enhanced or diminished by a substitution on the aromatic ring or terminal group of the amidic bond. Species labeled as **HFR**₃ and **FHR**₃ are two distinct conformers of the same structure. They correspond to local minima obtained by optimization of the two possible geometries (**HFH** and **FHH** in Fig. 2). In the **HFH** geometry, strong repulsive interactions between the fluorine and oxygen atoms were observed but no hydrogen bond in the *trans* form. However, one stabilizing C—H...F hydrogen bond and weaker repulsion forces were observed in the *cis* form. On the other hand, *trans* form of the **FHH** geometry is stabilized *via* two hydrogen bonds (C—H...O and N—H...F). *Cis* form contains only the N—H...F hydrogen bond. Considering the total electronic energies of optimized substituted molecules, the most probable conformers can be

determined. In Tab. 1, DFT values of total electronic energy and energy difference ΔE between *cis* and *trans* geometric isomers are presented. A negative value of ΔE indicates that the *cis* form is more energetically preferred. For the most studied compounds, *trans* form is favored; the only exception is fluorine-substituted 2-fluoroformanilide and 2,6-difluoroformanilide where *cis* form is more stable (**HFHc** and **FFHc**). In case of **FFHc**, two hydrogen bonds were identified between fluorine atoms of the aromatic ring and both hydrogens of the amidic group. Oxygen and fluorine atoms are highly electronegative and there are strong repulsive forces in the *trans* form of this molecule (as in **HFHt** and **FFHt**). According to the Boltzmann distribution, the population of **HFHt** and **FFHt** at 300 K is expected to be between 90 and 94 % compared to the *cis* forms. As shown in Fig. 2, a strong steric interaction between oxygen and fluorine atoms due to the *ortho*-fluorine substitution of formanilide causes an increase of the dihedral angle (from planar starting point) in **HFHt**. Dihedral angle C6—C1—N7—C8, which represents the rotation of the aromatic ring with respect to the —CO—NH— plane, reached the value of -123° in **HFHt**. Repulsive forces between oxygen and fluorine atoms in the *cis* form are suppressed because of greater distance between these atoms. In **HFHc**, also intramolecular hydrogen bonds between oxygen of the carbonyl group and o-hydrogen of phenyl were observed to stabilize the isomer. Moreover, experimentally significant population of the *cis* form (more than 5 %) at 300 K has been predicted also for **HHH**, **Me₂H**, **HFH**, **HFMe**, **HFF**, **HFCl**, **FFMe** and **FFF**. In case of **Me₂H** and

Table 1. Theoretical gas-phase B3LYP 6-311+G(3df,2p) total electronic energies of studied anilide derivatives. ΔE stands for energy difference between the *cis* and *trans* isomer.

Molecule	E_c /Hartree	E_t /Hartree	ΔE /kJ·mol ⁻¹	Molecule	E_c /Hartree	E_t /Hartree	ΔE /kJ·mol ⁻¹
HHH	-401.085091	-401.086621	4.0	FFH	-599.627578	-599.625540	-5.3
HHMe	-440.417791	-440.422353	12.0	FFMe	-638.960735	-638.962214	3.9
HHCCl₃	-1819.260603	-1819.274920	37.6	FFCCl₃	-2017.802910	-2017.813485	27.8
HHCF₃	-738.242430	-738.252430	25.9	FFCF₃	-936.784294	-936.790458	16.2
HHF	-500.376693	-500.381100	11.6	FFF	-698.917684	-698.919103	3.7
HHCl	-860.718387	-860.726063	20.2	FFCl	-1059.260470	-1059.264125	9.6
HHBr	-2974.636573	-2974.645182	22.6	FFBr	-3173.178655	-3173.183064	11.6
Me₂H	-479.741467	-479.741558	0.2	HFH	-500.355757	-500.353113	-6.9
FHH	-500.358168	-500.360875	7.1	HFMe	-539.689302	-539.689467	0.4
HFMe	-539.690501	-539.697041	17.2	HFCCl₃	-1918.532702	-1918.541863	24.1
FHCCl₃	-1918.532702	-1918.548374	41.1	HFCF₃	-837.514294	-837.518975	12.3
FHCF₃	-837.514294	-837.525665	29.9	HFF	-599.646544	-599.647589	2.7
FHF	-599.649916	-599.654581	12.2	HFCl	-959.990388	-959.992778	6.3
FHCl	-959.990388	-959.999312	23.4	HFBr	-3073.908333	-3073.911883	9.3
FHBr	-3073.908332	-3073.918233	26.0

Fig. 2 Top and side views of the optimal gas-phase B3LYP structures of **HFH**, **HHCl** and **FHH** isomers.

HFMe, the *cis/trans* ratio is nearly 50:50 due to the steric effect of the methyl group.

As it was mentioned earlier, in all studied cases with two exceptions discussed above, *trans* form is favored mainly because of hydrogen bonds between hydrogen and oxygen or fluorine atoms. These stabilizing interactions result in total planarity of the whole molecule with the C6—C1—N7—C8 dihedral angle of around 180°. On the other hand, dihedral angles of *cis* forms differ according to steric interactions and the volume of substituents at

the amide group. Large deflections of the dihedral angle from the C=O bond plane in molecules are caused by steric repulsive interactions and absence of hydrogen bonding (Fig. 2). In case of formanilide **HHH** and generally in molecules noted as **HHR₃**, the amide group is coplanar with the aromatic ring in *trans* conformers due to strong O···H hydrogen bonding. In case of the **HHH** molecule, both isomers are planar. Moreover, optimal geometries of *trans* isomers of all studied **FHR₃** molecules resulted in total planarity (studied dihedral angle was 180 °)

due to the presence of two strong hydrogen bonds between hydrogen, fluorine and oxygen atoms (see molecule **FHH** in Fig. 2).

Aromaticity HOMED indexes presented in Table 2 were calculated from bond lengths using Eq. 1 and Eq. 2 for B3LYP 6-311+G(3df,2p) optimized geometries. Conformational changes from the *cis* to the *trans* form cause the HOMED parameter value to change at most by 0.002, hence these changes can be considered as insignificant. It follows that intramolecular hydrogen bonds in formanilide derivatives stabilize the molecule, so aromaticity is preserved in all cases. As shown in Tab. 2, the most significant changes were observed for bonds *f* and *e* (Fig. 3), which are closest to the C=O bond and are mostly influenced by the *ortho* substitution of the phenyl ring. In case of **FHMe** and **FHBr**, significant elongation of bond length *b* up to 0.008 Å was predicted;

Fig. 3 General structure and bond labelling in the phenyl ring of the *trans* conformer.

The same notation was used for the *cis* isomers.

however, according to their ΔE values, settling of these molecules in the *cis* form is improbable.

Based on the normal mode analysis, two characteristic normal modes were identified: N—H and C=O stretching vibrations, which reflect the substitution effect and isomerism in all studied derivatives. This selection is in agreement with the theoretical *ab initio*

Table 2 Bond lengths (*a-f*) in aromatic ring of the studied molecules and HOMED parameters calculated according to Eq. 1. Parametrization constant α is equal to 87.108 (Eq. 2). Bond lengths are in Å.

Molecule	<i>a</i> /Å	<i>b</i> /Å	<i>c</i> /Å	<i>d</i> /Å	<i>e</i> /Å	<i>f</i> /Å	HOMED	Molecule	<i>a</i> /Å	<i>b</i> /Å	<i>c</i> /Å	<i>d</i> /Å	<i>e</i> /Å	<i>f</i> /Å	HOMED
HHHt	1.390	1.389	1.391	1.386	1.398	1.397	0.998	HHHc	1.389	1.390	1.390	1.387	1.397	1.398	0.998
HHMet	1.386	1.391	1.389	1.390	1.397	1.399	0.998	HHMec	1.387	1.391	1.389	1.389	1.396	1.398	0.999
HHCCl₃t	1.385	1.391	1.389	1.390	1.396	1.398	0.998	HHCCl₃c	1.388	1.391	1.389	1.390	1.390	1.393	1.000
HHCF₃t	1.386	1.391	1.389	1.390	1.396	1.397	0.999	HHCF₃c	1.388	1.391	1.389	1.390	1.391	1.393	1.000
HHFt	1.386	1.390	1.389	1.390	1.395	1.396	0.999	HHFc	1.387	1.390	1.389	1.389	1.394	1.396	0.999
HHCl_t	1.386	1.390	1.389	1.390	1.395	1.397	0.999	HHClc	1.390	1.390	1.391	1.388	1.392	1.392	1.000
HHBr_t	1.386	1.391	1.389	1.390	1.394	1.397	0.999	HHBrc	1.383	1.390	1.387	1.389	1.391	1.391	1.000
HFHt	1.388	1.390	1.389	1.383	1.391	1.394	0.999	HFHc	1.387	1.390	1.389	1.381	1.387	1.398	0.997
HFMet	1.388	1.390	1.389	1.383	1.392	1.394	0.999	HFMec	1.388	1.391	1.389	1.383	1.395	1.397	0.998
HFCCl₃t	1.388	1.390	1.389	1.383	1.394	1.393	0.999	HFCCl₃c	1.389	1.390	1.390	1.382	1.393	1.392	0.999
HFCE₃t	1.390	1.388	1.389	1.383	1.394	1.393	0.999	HFCE₃c	1.389	1.390	1.390	1.381	1.393	1.392	0.998
FFFt	1.388	1.390	1.389	1.383	1.392	1.392	0.999	FFFc	1.390	1.388	1.389	1.383	1.393	1.393	0.999
HFCl_t	1.388	1.390	1.389	1.383	1.393	1.393	0.999	HFClc	1.388	1.391	1.389	1.381	1.393	1.393	0.998
HFBrt	1.388	1.390	1.389	1.383	1.393	1.393	0.999	HFBrc	1.387	1.391	1.389	1.382	1.392	1.392	0.998
FHHt	1.385	1.392	1.389	1.390	1.397	1.396	0.996	FHHc	1.387	1.391	1.389	1.389	1.397	1.395	0.997
FHMet	1.376	1.382	1.389	1.391	1.397	1.397	0.996	FHMec	1.378	1.389	1.391	1.388	1.393	1.393	0.997
FHCCl₃t	1.376	1.391	1.389	1.390	1.396	1.396	0.996	FHCCl₃c	1.382	1.390	1.390	1.389	1.392	1.393	0.999
FHCE₃t	1.376	1.391	1.389	1.390	1.396	1.396	0.996	FHCF₃c	1.381	1.389	1.391	1.388	1.393	1.393	0.998
HFHt	1.377	1.391	1.389	1.390	1.395	1.395	0.997	HFHc	1.376	1.390	1.388	1.390	1.396	1.397	0.996
HFCl_t	1.376	1.391	1.389	1.390	1.395	1.395	0.996	HFClc	1.381	1.389	1.391	1.388	1.393	1.393	0.998
FHBr_t	1.376	1.381	1.389	1.39	1.395	1.395	0.996	FHBrc	1.382	1.389	1.391	1.388	1.392	1.392	0.998
FFHt	1.380	1.390	1.388	1.383	1.395	1.394	0.997	FFHc	1.378	1.390	1.388	1.382	1.396	1.398	0.995
FFMet	1.380	1.390	1.389	1.383	1.395	1.393	0.997	FFMec	1.380	1.390	1.389	1.383	1.396	1.398	0.996
FFCCl₃t	1.380	1.390	1.389	1.383	1.394	1.393	0.997	FFCCl₃c	1.382	1.389	1.389	1.382	1.396	1.396	0.997
FFCE₃t	1.380	1.390	1.389	1.383	1.394	1.393	0.997	FFCE₃c	1.382	1.389	1.389	1.382	1.395	1.395	0.997
FFFt	1.380	1.390	1.389	1.383	1.394	1.393	0.997	FFFc	1.381	1.390	1.389	1.382	1.395	1.394	0.997
FFCl_t	1.380	1.390	1.389	1.383	1.394	1.393	0.997	FFClc	1.382	1.389	1.389	1.382	1.395	1.394	0.997
FFBr_t	1.380	1.390	1.389	1.383	1.394	1.393	0.997	FFBrc	1.382	1.389	1.389	1.382	1.394	1.394	0.997
Me₂Ht	1.395	1.386	1.388	1.392	1.404	1.402	0.995	Me₂Hc	1.396	1.386	1.388	1.391	1.405	1.403	0.994

Fig. 4 Frequencies of N—H and C=O stretching modes obtained by the B3LYP/6-311+G(3df,2p) vibrational analysis; values were corrected by a factor of 0.8933 and compared with the experimental data (Ilieva et al., 1999; SDBSWeb, 2017).

Fig. 5 Visualization of the studied N—H and C=O vibrational modes of *trans* and *cis* formanilide (HHH). Both positive (blue) and negative (green) displacement vectors of the strongest vibrations are depicted.

4-31G calculations and experimental observations on a smaller set of anilide derivatives (Ilieva et al., 1999; SDBSWeb, 2017). All calculated and experimental stretching frequencies are presented in Fig. 4.

As shown in Fig. 5, the band around 3600 cm^{-1} corresponds to almost pure N—H stretching mode. On the other hand, the band at 1800 cm^{-1} consists of the C=O stretching mode and the C—H/N—H bending mode of the amidic group. Frequencies calculated for the N—H band in the range of $3557\text{—}3620\text{ cm}^{-1}$ corresponding to *cis* conformers are lower than those for the N—H band corresponding to *trans* forms of the molecule (interval $3590\text{—}3629\text{ cm}^{-1}$). A similar trend was observed for vibrational frequencies of the C=O band (calculated frequencies are in the interval of $1754\text{—}1900\text{ cm}^{-1}$ for *trans* form and between $1745\text{—}1881\text{ cm}^{-1}$ for *cis* form). The B3LYP calculated N—H stretching mode frequencies for different conformers of the studied molecules were compared with the experimental data depicted as horizontal lines in Fig. 4. The decrease in the N—H stretching mode frequencies in the *cis* structures was attributed to the direct field effect of the carbonyl group in the specific mutual orientation of the C=O and N—H bonds.

The DFT calculations predict almost identical absolute intensities for the N—H stretching vibra-

tions of formanilide and acetanilide associated with the N—H stretching vibrations of the *cis* and *trans* isomers. Therefore it can be assumed that the integrated intensities in the infrared spectra quantitatively reflect the *cis* and *trans* conformational forms concentrations. Experimental data have clearly shown that the higher frequency band at 3429 cm^{-1} in case of formanilide and at 3453 cm^{-1} in case of o-methylacetanilide, is more intense. Concentration of the *trans* isomer is also higher, which is in agreement with the *ab initio* estimated total energies showing higher stability of the *trans* conformers of formanilide and o-methylacetanilide (Ilieva et al., 1999). Additionally, it can be noted that experimental frequencies agree well with our corrected theoretically predicted frequencies.

Conclusions

Using the density functional theory, the acidic residue has been proved to influence the *cis/trans* equilibrium. A substitution on the phenyl ring modifies the intramolecular hydrogen bond formed between the amidic C=O group and the hydrogen atom of the aromatic ring. For the parent formanilide molecule, the energy of this interaction is around $4\text{ kJ}\cdot\text{mol}^{-1}$. Other hydrogen bonds were also identi-

fied for the fluorine atom substitution. The steric effect for methyl derivatives was quantified. The effect of the substitution on the aromaticity can be considered to be negligible given the invariance of HOMED index values of *cis* and *trans* isomers. The N—H and C=O stretching frequencies obtained by the vibrational analysis were compared with the experimental data. From the obtained results, it can be concluded that the applied computational method for the vibrational spectra prediction is reliable. The proposed stability predictions of anilide derivatives shed light on their reactivity and molecular shape, which can play supportive role in structure-based drug design through molecular docking or in the discovery of possible synthetic routes.

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