EVALUATION OF THE INFLUENCE OF THE SUPPLY PRESSURE ON FUNCTIONAL PARAMETERS OF THE IMPULSE LOW-PRESSURE GAS-PHASE INJECTOR

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Abstract: The article presents research results referring to the influence of supply pressure on the functional parameters of the impulse low-pressure gas-phase injector. The study was done on the original stand for flow test of gas-phase injectors. In the indirect evaluation, with the initial parameters and the length of the forced impulse, the current line, acceleration and pressure sensor courses were used. Apart from the volumetric flow rate, the analysed parameters were the time periods of the injector opening and closing process. Those time segments were composed of response time and opening/closing time, the sum of which gives time of full opening. Functional relationships describing the volumetric flow rate, time of full opening and closing are presented, which are helpful not only in comparative tests of different injectors, but also in modelling the operation of gas injector or algorithms of gas supply control system. The reference to the volumetric flow rate allowed to indicate possible causes of variability of this parameter depending on the supply pressure.

Key words: Mechanical engineering, combustion engines, fuel supply, alternative fuel injector, research

1. INTRODUCTION

In recent years, we have seen legislative efforts to reduce exhaust emissions from engines used in transport (WLTP, 2019). This is generally known as greenhouse gases (GHGs) (Clairotte et al., 2020). Although some of the regulations are European, manufacturers around the world are adapting their engines to the requirements of the next Euro emission limits, considering distribution issues (Kim et al., 2020). In 2018, CO₂ emissions during a European car certification test could reach 120.5 g/km. Since 2020, this has been reduced to 95 g/km. In a longer-term perspective, further reductions by 15% in 2025 and 37.5% in 2030 are planned (García et al., 2020). Such actions will most probably exclude the possibility of using combustion engines as the only source of vehicle propulsion. However, they may still be used in hybrid systems with different connection configurations (Raslavičius et al., 2015, 2017). A separate issue proposed for inclusion in the future Euro VII standard is the unification of exhaust emissions for cars, vans, and trucks. There are still matters of emissions for machines and non-road vehicles (Waluś et al., 2018; Warguła et al., 2018).

In Europe, the most popular alternative fuel used in cars and vans is liquefied petroleum gas (LPG) (Raslavičius et al., 2014). Alternative fuels are listed in the European Union Directive (2014/94/EU) (Council of the European Union, 2014). Interest in using LPG/CNG in forklift and working machinery engines is also observed (Warguła et al., 2020, 2020a).

Taking into consideration the emission regulations, more precise algorithms are required to monitor the performance of the internal combustion engine, and in particular towards the gas fuel supply (Dziewiatkowski et al., 2020). More precise executive modules are also required (Szpica, 2016). Additionally, it is necessary to know the working characteristics of the components in relation to variable input parameters.

The impulse low-pressure gas-phase injectors, which are installed in alternative combustion engine supply systems, are characterized by their diverse design. Out of many parameters, which can describe the operation of the gas injector, the volumetric flow rate (Czarnigowski, 2012) and the time periods associated with the movement of the actuator (Duk and Czarnigowski, 2012; Szpica, 2018) are considered as basic.

For the functional evaluation of the gas injectors, computational methods used for modelling the operation of engines and their components may be used:

- 0-D modelling (Baldi et al., 2015; Feng et al., 2019; Ngayihi Abbe et al., 2015; Polášek et al., 2002);
- 1-D modelling (Cerri et al., 2006; Da Silva Trindade and Dos Santos, 2016; Sawant and Bari, 2017; Pauras Sawant et al., 2018);
- 3-D modelling (Broatch et al., 2019; Buhl et al., 2017; Kosmadakis et al., 2012; Mohammadi et al., 2012).

Calculation methods are becoming essential when prototyping new construction solutions. Analytical models are used here (Brumercik et al., 2020; Szpica and Kuszniier, 2020). For strength

and thermal evaluation, the finite element method (FEM) is widely used (Bensetti et al., 2006; Borawski et al., 2020, 2021), while in the flow part, computational fluid dynamics (CFD) (Czarnigowski et al., 2007, 2009; Marčić et al., 2015; Szpica, 2015). A very difficult computational problem is the phenomenon of circuit magnetism with an injector drive coil (Passarini and Nakajima, 2003; Passarini and Pinotti, 2003; Taghizadeh et al., 2009). In gas injectors, as in other fuel injectors, there are high hopes for piezo-electric propulsion (Mieczkowski, 2019; Mieczkowski et al., 2020; Pogulyaev et al., 2015; Satkoski et al., 2009).

Mathematical modelling allows for the approximation of real processes, but in effect, experimental verification is required. For testing gas injectors, experimental methods used for functional analysis of injectors for different fuels can be applied:

- high speed cameras (Aleiferis et al., 2010; Jang et al., 2000; Panão and Moreira, 2005);
- optical laser (Kakuhou et al., 1999; Leach et al., 2007; Robart et al., 2001);
- light fluorescence absorption (Aleiferis and Van Romunde, 2013; Leach et al., 2007);
- current in the power line (Duk and Czarnigowski, 2012; Szpica, 2018);
- heat flow sensors (Serras-Pereira et al., 2013);
- acceleration sensors (Czarnigowski, 2012; Szpica, 2018);
- pressure sensors (Duk and Czarnigowski, 2012; Szpica, 2018);
- lift sensors (Ambrozik and Kurczyński, 2008; Szpica, 2018);
- optical sensors (Walaszyk and Busz, 2013);
- gravimetric method (Szpica and Czaban, 2014);
- ‘fuel tank refill’ method (Szpica and Czaban, 2014).

The methods presented above differ in the level of complexity, the required equipment, as well as the way they interfere with the executive parts. The use of direct methods gives the most precise picture of the processes, but this often involves interfering with the working system, which must be repaired at a later stage. As shown in (Szpica, 2018) indirect methods, which exclude interference with the working elements of the gas injector, also allow for a correct assessment of functional parameters.

On the one hand, the emission regulations and, on the other hand, the expansion of the control algorithms within the engine require knowledge not only of the static characteristics, but also of their changes when adjusting the input parameters. The main feature of the injector, which is the volumetric flow rate, has been improved by time intervals for opening and closing the injector, filling the research gap in this area. The aim of the study was to develop functional dependencies describing the variability of the analysed parameters that may be helpful in the analysis of engine transitions as well as in creating mathematical models.

2. THE RESEARCH OBJECT

The object of the research was STAG AC W02 – four-section injection rail LPG/CNG (Fig. 1a). W02 is the impulse low-pressure gas-phase injector. In the lack of power supply, plunger 1 (Fig. 1b) is pressed against the socket by spring 3 and gas flow is not possible. When an electrical impulse arises in circuit 2, the electromagnetic force raises plunger 1 and the gas flow is realized according to the red arrows (Fig. 1). When the electric impulse disappears, spring 3 moves plunger 1 downwards, making the flow impossible.

Fig. 1. STAG AC W02 – four-section injection rail LPG/CNG: a – picture; b – scheme: 1 – plunger, 2 – electromagnetic circuit, 3 – spring, red arrows point at the flow direction

Basic technical data of the STAG AC W02 – four-section injection rail LPG/CNG have been presented in Tab. 1.

Tab. 1. Basic technical data of the Valtek Rail Type 30 gas injector
Data taken from (AC, 2020)

Parameter	Value
max flow rate at 1.2 bar	120 NL/min
coil resistance	1.9 Ω
nozzle size	(min 1.5/max 2.8) mm
opening time/closing time	(2 / 1) ms
operating temperature	(–20 ÷ 120)°C
max working pressure	400 kPa

3. THE RESEARCH METHODOLOGY

The tests were carried out on the original gas injector flow test stand. For safety reasons, the tests were conducted using air instead of LPG/CNG (Fig. 2). In the evaluation of functional parameters, indirect methods were used without interfering with the injector's working system.

Compressed air from air supply 1 flows through the air preparation 2 system to the buffer tank 3. The buffer tank is designed to accumulate sufficient air to prevent temporary pressure drops. The air continues to flow through the tested injector 4. The impulse action of the injector is controlled by a pulse generator 5.

Fig. 2. The scheme of the measurement stand: 1 – air supply, 2 – air preparation system, 3 – buffer tank, 4 – tested injector, 5 – pulse generator (based STAG ECU), 6 – voltage connector, 7 – current lines, 8 – accelerometer, 9 – pressure gauge, 10 – oscilloscope, 11 – mass flow meter, 12 – multimeter

In the measurement section that assesses the power supply, there is a voltage connector 6 and current line 7. The return positions of the injector plunger are accompanied by vibrations, which are read out by the accelerometer 8. The air stream coming out of the injector under test goes to the pressure sensor 9, which estimates the operating cycle in terms of flow-through. The design and operation of pressure sensor 9 is described in Szpica (2018).

Signals are stored in oscilloscope 10. In addition, it is possible to measure the average injector output through the mass flow meter 11 and multimeter Brymen 907 12. Basic technical data of the measurement equipment have been presented in Tab. 2.

By using an oscilloscope, it was possible to register 4 different channels. Assuming that the voltage supply to the injector is forced, the corps acceleration, current line, and pressure are additionally recorded. The registered values were saved to *.csv file. The results were processed using software created in Guide

Matlab-Simulink. A Butteworth low pass filter (Yang et al., 2005) was used to filter the waveforms. As a result, it was possible to read the times describing the injector reaction when opening and closing (Fig. 3). Based on the 'breakthrough' of the current line, only the time to full opening (t_{fo}) could be read. The acceleration course and the pressure course made it possible to read both response of opening or closing time (t_{or} , t_{cr}) and opening time (t_o) or closing time (t_c). By adding up response time and opening/closing time as a result, we get time to full opening/closing.

Tab. 2. Parameters of the measuring equipment

Parameter	Measurement device	Response time	Range	Output signal	Accuracy
current	HAMEG HZ050	< 1 μ s	± 30 A	100 mV/A	1%
acceleration	KELAG KAS903-02A	< 1 ms	± 12 g	(0.5–4.5) V	0.005 g
pressure	MPXH6400A	< 1 ms	(20–400) kPa	(0–5) V	0.25%
mass flow	BRONKHORST F-113AC-M50-ABD-00-V	< 0.5 s	(0–300) Nl/min	(0–5) V	0.5%
voltage	RIGOL RP1500A	bandwidth ~ 150 MHz; damping factor – 10:1			
record	RIGOL MSO4014	bandwidth – 100 MHz; real-time sample rate – up to 4 GSa/s

Fig. 3. Example courses recorded during the measurement (injection impulse 10 ms, PWM after 3 ms): t – time; index: or – of opening response, o – of opening, fo – of full opening, cr – of closing response, c – of closing

4. RESULTS OF THE MEASUREMENT

In the initial part of the study, the volumetric flow rate was determined using the flow meter. The supply pressure regulated in the scope (0.5–2.5) e5 Pa. The pulse generator has been set with constant parameters: frequency of impulses: 1000 min⁻¹; injection time: 10 ms; signal modulation 90% PWM at 3 ms; voltage: 14 V; outlet nozzle diameter: 3.2 mm.

The variability of volumetric flow rate relative to supply pressure was presented in the Fig. 4. The relation $Q = f(p)$ was approximated with the polynomial of 3rd degree:

$$Q = -1.1612p^2 + 13.9160p + 1.2933 \quad (R^2 = 99.9\%) \quad (1)$$

It was found that a 9-fold increase in supply pressure results in an approximate 6-fold increase in volumetric flow rate, the ratio is not proportional. In the study (Czarnigowski, 2012), the results of the volumetric flow rate tests of constructively similar injectors were presented. Despite the differences in values, the variability of the tested parameters correlates with the one presented in this study.

Fig. 4. The relation of the volumetric flow rate and the supply pressure for the tested injector

In order to maintain the necessary relationship towards comparison, the variability of time characterizing the injector operation was also approximated with the polynomial of 3rd degree. Functional dependencies have been determined for time to full opening and full closing. Full opening time based on the current course was described (Fig. 5a)

$$t_{fo} = -0.0358p^2 + 0.3066p + 1.4355 \quad (R^2 = 99.7\%) \quad (2)$$

and the acceleration sensor course

$$t_{fo} = -0.0485p^2 + 0.3263p + 1.5380 \quad (R^2 = 99.5\%) \quad (3)$$

also the pressure sensor course

$$t_{fo} = -0.0200p^2 + 0.2308p + 1.7478 \quad (R^2 = 99.1\%) \quad (4)$$

In case of evaluation of the injector closing process, it is im-

possible to evaluate it on the basis of the current line. Therefore, the ratios defining time to full closing are described based on the acceleration sensor course (Fig. 5d)

$$t_{fc} = 0.0109p^2 - 0.1102p + 2.3383 \quad (R^2 = 95.0\%) \quad (5)$$

and the pressure sensor course

$$t_{fc} = 0.0333p^2 - 0.0531p + 2.3498 \quad (R^2 = 82.9\%) \quad (6)$$

Fig. 5. The results of the research: a – time to full opening, b – opening response time, c – opening time, d – time to full closing, e – response closing time, f – closing time

In the case of time to full opening variability, it was found that a 9-fold increase in supply pressure gives time to full opening increments in the range 20–32%, current line – 32%, acceleration sensor – 28% and pressure sensor – 21% accordingly. Analysing Fig. 5b and c, the dominant influence of opening response time is observed. It results from the necessity to overcome the force from the differential pressure above and below the piston by the electromagnetic force of the drive. The opening process itself is characterized by similar time values, due to the disappearance of the pressure difference under and over the piston.

The closing process of the injector and the associated characteristic times are more difficult to estimate using indirect methods. While the acceleration sensor shows a 7.5% decrease in time to full closing, the pressure sensor shows a 2% increase. In this case, the accelerator sensor should be considered as representative, because in the pressure sensor and its course of pressure in the process of closing the injector, there is still a phase of air stream expansion between the injector and the sensor, as described in Szpica (2018). On the basis Fig. 5e and f for the acceleration sensor, it is possible to state the major influence of response time on time to full closing.

The presented results of research on the influence of supply pressure on functional parameters of the impulse low-pressure gas-phase injector correlate with the research and conclusions from the experimental studies presented in (Czarnigowski, 2010, 2014). It was found there that the supply pressure has an impact

on the opening response time because, as already mentioned, the electromagnetic force has to overcome the greater pressure difference under and over the piston. However, there was no confirmation with reference to the characteristic times of the opening and closing process. An analysis of opening and closing times of the injector can be helpful in developing an algorithm to control the operation of the supply system at variable gas pressure regarding the change in injection angle.

The results obtained in the course of the research are also the base for the verification of mathematical models describing the operation of the gas injector, for example Szpica and Kuszner (2020).

5. CONCLUSIONS

The studies presented in the article and their analysis were intended to evaluate the influence of supply pressure on the functional parameters of the impulse low-pressure gas-phase injector. The parameters evaluated were volumetric flow rate and time intervals describing the process of opening and closing the injector. The conclusions are as follows,

- A 9-fold increase of supply pressure gives a 6-fold increase in the volumetric flow rate. The relation was approximated with the polynomial of 3rd degree;

- Changes in supply pressure in the scope covered by the research plan result in time to full opening increases of a range 20–32%.
- The opening response time has a more significant impact on the time to full opening than opening time.
- The acceleration sensor shows a 7.5% decrease in time to full closing, with a significantly higher impact on response time than closing time.
- The pressure sensor gives a 2% increase in time to full closing, but its course during closing process is not fully representative, which takes into account the expansion phase of the stream between injector and sensor.

The study results presented in the article fill the research gap regarding the evaluation of the influence of supply pressure on the examined time periods. They are also helpful in creating mathematical models describing the operation of the gas injector or planning algorithms for controlling the gas supply system. In the next stage, it is planned to verify the research presented in the study by the direct method using the displacement sensor.

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